# Experimental Study of Equilibria in the $Ta_2O_5$ -Fe-Fe<sub>2</sub>O<sub>3</sub> System at 1200°C

## **KENZO KITAYAMA**

Department of Chemistry, Faculty of Science, Tokyo Institute of Technology, Ookayama, Meguro-ku, Tokyo 152

Received October 25, 1985; in revised form January 27, 1986

Phase equilibria in the system  $Ta_2O_5$ -Fe-Fe<sub>2</sub>O<sub>3</sub> were established at 1200°C by changing the oxygen partial pressure from 0 to 16.60 in  $-\log (P_{O_2}/atm)$ . In this system FeTaO<sub>4</sub>, FeTa<sub>2</sub>O<sub>6</sub>, and Fe<sub>4</sub>Ta<sub>2</sub>O<sub>9</sub> are stable in addition to the well known two compounds in the Fe-Fe<sub>2</sub>O<sub>3</sub> system. These compounds have nonstoichiometric compositions. In particular, FeTaO<sub>4</sub>, FeTa<sub>2</sub>O<sub>6</sub>, and a spinel solid solution, which have an end member Fe<sub>3</sub>O<sub>4</sub>, have a considerable wide range of nonstoichiometry. Lattice constants of the compounds and the solid solutions which appeared in the system were also determined and discussed with respect to their dependence on the atmosphere in which the samples were made. By calculating the activities of each component in the above solid solutions, the standard Gibbs energies of reactions, (1) Fe + Ta<sub>2</sub>O<sub>5</sub> +  $\frac{1}{2}O_2 = FeTa_2O_6$ , (2) 2FeTa<sub>2</sub>O<sub>6</sub> +  $\frac{1}{2}O_2 = 2FeTaO_4 + Ta_2O_5$ , (3) FeTa<sub>2</sub>O<sub>6</sub> +  $\frac{3}{2}Fe + \frac{3}{2}O_2 = Fe_4Ta_2O_9$ , and (4) Fe<sub>4</sub>Ta<sub>2</sub>O<sub>9</sub> +  $\frac{1}{2}O_2 = FeTa_2O_6 + Fe_3O_4$ , were calculated as -221.4, -6.8, -522.4, and -133.7 kJ, respectively. @ 1986 Academic Press, Inc.

There are several previous publications on the double oxides involving the Ta oxides (1-3). These works principally treated natural tantalate minerals (1) and were performed from the viewpoint of the structure of compounds formed by solid reactions (2-4) and of the physical properties (5, 6). In these studies (2, 3), the double oxides, Fe-TaO<sub>4</sub> and FeTa<sub>2</sub>O<sub>6</sub>, were found to be stable.

Subsolidus phase relations of the oxides in the system Fe-Ta-O were experimentally determined at 1200°C under conditions of the variable oxygen partial pressure by Turnock (7). In that report the following ternary compounds were synthesized: Fe<sub>4</sub> Ta<sub>2</sub>O<sub>9</sub> and Fe<sub>3</sub>Ta<sub>2</sub>O<sub>8.1</sub> in addition to Fe TaO<sub>4</sub> and FeTa<sub>2</sub>O<sub>6</sub>, a solid solution between these two compounds, and tantalian magnetites. However, these results are insufficient for a complete understanding of the phase equilibria. For example, since the quench method was adopted, the isothermal projection of the Fe-Ta-O system (Fig. 1 in (7)) would be uncertain and the oxygen partial pressure in equilibrium with three-solid phases would be in much error (Table II in (7)). Therefore, thermochemical data for the reactions found in the system were not calculated successfully. In view of the uncertainty in the system arising from the results in the literature, further investigation seemed desirable to understand the phase relations more completely.

#### Experimental

Guaranteed reagent grade  $Fe_2O_3$  (99.9%) and  $Ta_2O_5$  (99.9%), which were previously

dried, were used for starting materials.  $Ta_2O_5$  is a very stable oxide with a melting point of 1877  $\pm$  5°C and exists in two distinctly different crystalline forms with a quenchable phase transition at ~1350°C (8). It was confirmed on preliminary experiments that  $Ta_2O_5$  was stoichiometric in the present experimental conditions.

Desired ratios of  $Ta_2O_5/Fe_2O_3$  were obtained by mixing thoroughly in an agate mortar under ethyl alcohol. The mixtures thus obtained were treated by the same procedures as in the previous paper (9). The apparatus and procedures for controlling the oxygen partial pressure and keeping a constant temperature, the method of the thermogravimetry, and the criterion for establishing equilibrium were the same as those described in the previous papers (9– 11).

# **Results and Discussions**

### Phase Equilibria

The Fe-Fe<sub>2</sub>O<sub>3</sub> system, which is the partial system of the present one, was reinvestigated to confirm the calibration of the apparatus used. The results obtained were in good agreement with those of Darken and Gurry (12, 13).

Ten samples with  $Ta_2O_5/Fe_2O_3$  mole ratios of 8/2, 7/3, 5/3, 1, 4/6, 3/7, 2/8, 15/85, 1/9, and 5/95 were prepared to be used in the thermogravimetry.

In Fig. 1 the relationships between the oxygen partial pressure,  $-\log (P_{O_2}/\text{atm})$ , on the ordinate and the weight change,  $W_{O_2}/W_T$ , on the abscissa are shown with four representative samples, 7/3 (a), 4/6 (b), 2/8 (c), and 1/9 (d). Here,  $W_{O_2}$  is the weight decrease of the samples from the reference weight in 1 atm O<sub>2</sub>, and  $W_T$  is the total weight decrease of the sample which might be expected if all the Fe<sub>2</sub>O<sub>3</sub> in the sample changes to Fe-metal in H<sub>2</sub> atmosphere, for each sample. The  $W_{O_2}/W_T$  ratio in the present experiment usually had values in

the range from 0.998 to 1.000 in the atmosphere of H<sub>2</sub>. Therefore, the procedures might be reasonable in the present experiment. From Fig. 1 and referring to previous data (12, 13), the oxygen partial pressures in equilibrium with three-condensed phases or two-condensed phases are found as 2.94, 3.80, 6.70, 9.14, 9.72, 11.94, 12.00, 12.35, and 15.60 in  $-\log P_{O_2}$ .

The identification of the phases was done with quenched samples using a powder X-ray diffractometer with FeK $\alpha$  radiation. The following phases occur under the present experimental conditions: Ta<sub>2</sub>O<sub>5</sub>(B), FeTaO<sub>4</sub>(R), FeTa<sub>2</sub>O<sub>6</sub>(T), Fe<sub>4</sub>Ta<sub>2</sub>O<sub>9</sub>(S), Fe<sub>3</sub>O<sub>4</sub>(M), Fe<sub>2</sub>O<sub>3</sub>(H), "FeO"(W), and Fe. The results of the phase identification are shown in Table I in the form of the twophase combinations except for a few samples.

Based upon the above experimental results of the thermogravimetry and the identification of phases, a phase diagram can be drawn and is shown in Fig. 2. The present diagram is more simple than that of Turnock (7) which can be seen in Fig. 3. This figure was redrafted from the original one by the author in the same form as that of Fig. 2 to facilitate comparison of both diagrams.

Figure 2 is considerably different from that of Turnock: (1) The phase N, Fe<sub>3</sub> Ta<sub>2</sub>O<sub>8.1</sub>, is not stable and (2) the tantalian magnetite solid solution is stable but the width of its homogeneity range is not as wide as he had presented. It must be more narrow, considering the other present results, for example, the composition of  $M_6$ , Table II, and the constancy of the  $W_{O_2}/W_T$  of the sample 1/9 in the oxygen partial pressure range from 8.75 to 9.70 in -log  $P_{O_2}$ , Fig. 1d.

From (1) above, no three-condensed phase area exists which contains phase N. The three-solid phase area, Sp + Fe

 $Ta_2O_6$  + FeTaO<sub>4</sub>, corresponding to the No. 3 area of Turnock, was difficult to find be-

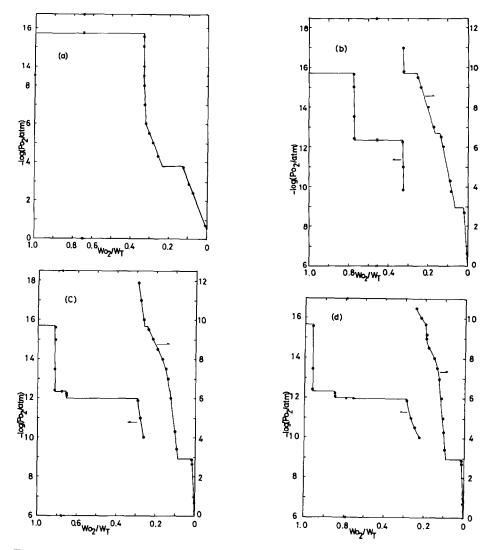


FIG. 1. The relationship between the oxygen partial pressure,  $-\log (P_{0_2}/atm)$ , and the weight change of the samples,  $W_{0_2}/W_T$ . (a)  $Ta_2O_5/Fe_2O_3 = 7/3$ , (b)  $Ta_2O_5/Fe_2O_3 = 4/6$ , (c)  $Ta_2O_5/Fe_2O_3 = 2/8$ , (d)  $Ta_2O_5/Fe_2O_3 = 1/9$ .

cause of the sluggish reaction in the range of high  $P_{O_2}$  and in the short range of the abrupt weight change. The existence of the area was confirmed by the results shown in Fig. 1b and by the identification of the phases. It can be seen by a small gap in the weight change between 7.00 and 6.50 in  $-\log P_{O_2}$  in Fig. 1b although the gap is not clear in Figs. 1c and d. Also the change in the two-phase combinations can be found from  $\text{FeTa}_2\text{O}_6 + Sp$  at  $-\log P_{\text{O}_2} = 7.00$  to  $\text{FeTaO}_4 + Sp$  at  $-\log P_{\text{O}_2} = 6.50$  in the samples 1/9 and 2/8.

It is very difficult to determine the twophase line, from Fe to  $M_6$ , on account of the small difference in the adjacent equilibrium oxygen partial pressure, 12.00 and 11.94 in  $-\log P_{O_2}$ .

Ta <sub>2</sub> O <sub>5</sub> /Fe <sub>2</sub> O <sub>3</sub> (mole ratio)	$-\log P_{O_2}$ (atm)	Time (hr)	Phase
8/2	16.60	8	Fe + $Ta_2O_5^a$
	13.50	7	$Ta_2O_5 + FeTa_2O_6$
	5.00	46	$Ta_2O_5 + FeTa_2O_6$
	3.60	39	Ta <sub>2</sub> O <sub>5</sub> + FeTaO <sub>4</sub>
1	16.60	8	$Fe + Ta_2O_5$
	13.50	7	Fe + FeTa <sub>2</sub> O <sub>6</sub>
	12.20	7	$FeTa_2O_6 + Fe_4Ta_2O_9$
	10.00	16	$FeTa_2O_6 + Fe_4Ta_2O_9$
	9.50	16	$Sp + FeTa_2O_6$
3/7	11.90	14	$Sp + Fe_4Ta_2O_9$
	10.00	22	$Sp + Fe_4Ta_2O_9$
	9.00	22	$Sp + FeTa_2O_6$
	6.50	19	Sp + FeTaO₄
	5.00	46	Sp + FeTaO <sub>4</sub>
	2.40	41	$Fe_2O_3 + FeTaO_4$
2/8	13.50	7	$Fe + FeTa_2O_6$
	12.20	7	Fe + Fe <sub>4</sub> Ta <sub>2</sub> O <sub>9</sub>
	11.90	14	Sp + Fe₄Ta <sub>2</sub> O <sub>9</sub>
	10.50	13	$Sp + Fe_4Ta_2O_9$
	9.00	14	$Sp + FeTa_2O_6$
	7.00	17	$Sp + FeTa_2O_6$
	6.50	19	Sp + FeTaO₄
1/9	11.97*	6	Sp + Fe + (FeO)
	9.00	22	Sp
	7.00	17	$Sp + FeTa_2O_6$
	6.50	19	Sp + FeTaO₄
5/95	11.97 <sup>b</sup>	6	Sp + Fe + (FeO)
	11.90	14	Sp + FeO
	9.20	31	Sp
	9.00	22	Sp
	8.00	24	$Sp + FeTa_2O_6$

TABLE I The Identification of Phases

<sup>a</sup> Low-temperature form (8).

<sup>b</sup> The mixture of Fe +  $Fe_4Ta_2O_9$  was used as the starting material.

" Trace "FeO" was found sometimes.

The end and intermediate compositions of the solid solutions were graphically determined after finishing the thermogravimetric experiments. The compositions of the end members of the solid solutions,  $T_4$ and  $R_3$ , are in considerable doubt because of the reasons described above. These results are shown in Table II together with the symbol, the activity, and the oxygen partial pressure in which these compounds are stable.

Turnock (7) had shown three two-phase areas resulting from a six-angled spinel solid solution area, but these two-phase areas could not be found in the present diagram.

Lattice constants of the compounds are tabulated in Table III. These values are not affected by the coexisting compounds, which are shown in the fourth column, judging from values of FeTa<sub>2</sub>O<sub>6</sub> at log  $P_{O_2} =$ -12.20, of FeTaO<sub>4</sub> at log  $P_{O_2} = 0$ , of Fe<sub>4</sub>  $Ta_2O_9$  at log  $P_{O_2} = -11.90$ , and of Sp at log  $P_{02} = -11.90$ . This fact might suggest that nonstoichiometry of the respective compounds toward the coexisting compounds does not exist or is very small. However, these lattice constants depend upon the atmosphere in which the compounds were prepared. This is very reasonable because the oxygen partial pressure changes the composition in this case. The lattice constants decrease with the increase of the oxygen partial pressure, for example, in the case of FeTa<sub>2</sub>O<sub>6</sub> and the spinel solid solution, and increase with the increase of the oxygen partial pressure, for example, in the case of FeTaO<sub>4</sub>. The variation of the lattice constant of the spinel solid solution with the oxygen partial pressure in equilibrium is shown in Table III and is illustrated in Fig.

TABLE II Compositions of Compounds, Symbols, Activities and Related Oxygen

PARTIAL PRESSURES

Component			$-\log P_{O_2}$	
<i>(i)</i>	Composition	Symbol	(atm)	$\log a_i$
FeTa <sub>2</sub> O <sub>6</sub>	FeTa <sub>2</sub> O <sub>6.00</sub>	Т	15.70-8.00	0
	FeTa <sub>2</sub> O <sub>6.00<sup><i>a</i></sup></sub>	$T_1$	12.35	~0
	FeTa <sub>2</sub> O <sub>6.00</sub> <sup>a</sup>	$T_2$	9.72	~0
	FeTa <sub>1.69</sub> O <sub>5.37</sub>	$T_3$	3.80	0.83
	FeTa <sub>1.61</sub> O <sub>5.20</sub>	$T_4$	6.70	1.26
FeTaO₄	FeTaO <sub>4.00</sub>	R	0-0.50	—
	FeTa <sub>1.08</sub> O <sub>4.17</sub>	$R_1$	2.94	
	FeTa <sub>1.41</sub> O <sub>4.82</sub>	$R_2$	3.80	0
	FeTa <sub>1.47</sub> O <sub>4.95</sub>	$R_3$	6.70	-0.29
Fe₄Ta <sub>2</sub> O <sub>9</sub>	Fe <sub>4</sub> Ta <sub>2</sub> O <sub>9.00</sub>	S	12.35	0
	$Fe_4Ta_2O_{9.08}$	<b>S</b> <sub>1</sub>	9.72	-0.052
Fe₃O₄	Fe <sub>3</sub> O <sub>4.04</sub>	$M_1$	2.94	-0.062
	Fe <sub>3</sub> O <sub>4.01</sub>	$M_2$	6.70	-0.010
	Fe <sub>3</sub> O <sub>4.00</sub>	М	9.14	0
	Fe <sub>2.88</sub> Ta <sub>0.15</sub> O <sub>4.00</sub>	$M_3$	9.14	0
	Fe <sub>2.64</sub> Ta <sub>0.39</sub> O <sub>4.00</sub>	$M_4$	9.72	-0.17
	Fe <sub>2.54</sub> Ta <sub>0.51</sub> O <sub>4.00</sub>	$M_5$	11.94	-0.93
	Fe <sub>2.54</sub> Ta <sub>0.51</sub> O <sub>4.00</sub> <sup>a</sup>	$M_6$	12.00	-1.09

<sup>a</sup> The composition does not change with the oxygen partial pressure.

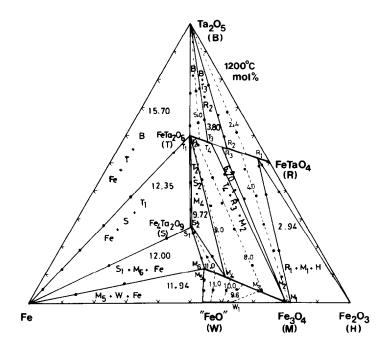


FIG. 2. Phase equilibria in the Ta<sub>2</sub>O<sub>5</sub>-Fe-Fe<sub>2</sub>O<sub>3</sub> system at 1200°C. Numerical values in the threesolid phase regions are the oxygen partial pressures in  $-\log (P_{O_2}/\text{atm})$  in equilibrium. Symbols are the same as those in Table II. The dotted lines in the two-solid phase areas are the iso-oxygen partial pressure lines shown by numerical values on the lines.

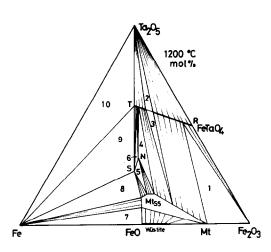


FIG. 3. Phase equilibria in the  $Ta_2O_5$ -Fe-Fe<sub>2</sub>O<sub>3</sub> system at 1200°C by Turnock. The diagram was redrafted in the same form as that of Fig. 2. Numbers in the three-solid phase areas and symbols of compounds correspond to those in the original diagram.

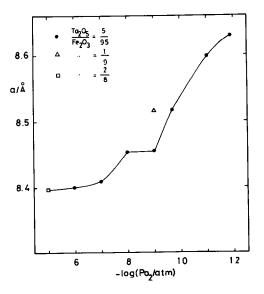


FIG. 4. The relationship between the lattice constant of the spinel solid solution and the oxygen partial pressure.

Compound	Ta <sub>2</sub> O <sub>5</sub> /Fe <sub>2</sub> O <sub>3</sub> (mole ratio)	$-\log P_{O_2}$ (atm)	Other phase	a (Å)	c (Å)	V (Å <sup>3</sup> )	Ref.
FeTa <sub>2</sub> O <sub>6</sub>	2/1	12.20		$4.775 \pm 0.001$	$9.199 \pm 0.004$	$208.0 \pm 0.1$	Present
	7/3	12.20	Ta <sub>2</sub> O <sub>5</sub>	$4.756 \pm 0.001$	$9.199 \pm 0.003$	$208.1 \pm 0.1$	Present
	5/3	12.20	Fe <sub>4</sub> Ta <sub>2</sub> O <sub>9</sub>	$4.756 \pm 0.001$	$9.203 \pm 0.003$	$208.1 \pm 0.1$	Present
	8/2	5.00	$Ta_2O_5$	$4.744 \pm 0.001$	$9.192 \pm 0.002$	$206.9 \pm 0.1$	Present
				$4.7451 \pm 0.0004$	9.179 ± 0.001		(5)
				4.750	9.205		(2)
FeTaO₄	3/7	6.00	Sp	$4.716 \pm 0.001$	$3.063 \pm 0.001$	$68.10 \pm 0.02$	Present
	3/7	5.00	Sp	4.697 ± 0.001	$3.055 \pm 0.001$	$67.41 \pm 0.02$	Present
	8/2	3.70	Ta <sub>2</sub> O <sub>5</sub>	$4.717 \pm 0.001$	$3.062 \pm 0.001$	$68.13 \pm 0.01$	Present
	8/2	2.40	Ta <sub>2</sub> O <sub>5</sub>	$4.703 \pm 0.002$	$3.044 \pm 0.005$	$67.3 \pm 0.1$	Present
	9/11	0	Fe <sub>2</sub> O <sub>3</sub>	$4.679 \pm 0.001$	$3.048 \pm 0.001$	$66.73 \pm 0.03$	Present
	1	0	_	$4.684 \pm 0.001$	$3.046 \pm 0.002$	$66.83 \pm 0.05$	Present
				4.708	3.075		(2)
				$4.678 \pm 0.002$	$3.048 \pm 0.004$		(7)
Fe₄Ta <sub>2</sub> O <sub>9</sub>	1/2	11.90	_	$5.230 \pm 0.001$	$14.226 \pm 0.002$	$336.9 \pm 0.1$	Present
	3/7	11.90	Sp	$5.230 \pm 0.002$	$14.220 \pm 0.005$	$336.8 \pm 0.2$	Present
	4/6	11.90	FeTa₂O <sub>6</sub>	$5.228 \pm 0.002$	$14.239 \pm 0.006$	$337.1 \pm 0.3$	Present
				5.224	14.202		(7)
Spinel	5/95	11.90	FeO	$8.629 \pm 0.002$		$642.4 \pm 0.4$	Present
opmor	2/8	11.90	Fe₄Ta <sub>2</sub> O <sub>9</sub>	$8.633 \pm 0.002$		$643.5 \pm 0.2$	Present
	5/95	11.00	FeO	$8.599 \pm 0.002$		$635.5 \pm 0.4$	Present
	5/95	9.70	FeO	$8.515 \pm 0.001$		$617.3 \pm 0.2$	Present
	1/9	9.00	FeTa <sub>2</sub> O <sub>6</sub>	$8.518 \pm 0.001$		$618.0 \pm 0.1$	Present
	5/95	9.00	_	$8.456 \pm 0.001$		$604.4 \pm 0.1$	Present
	5/95	8.00	FeTa <sub>2</sub> O <sub>6</sub>	$8.453 \pm 0.001$		$604.1 \pm 0.1$	Present
	5/95	7.00	FeTa <sub>2</sub> O <sub>6</sub>	$8.409 \pm 0.001$		$594.6 \pm 0.2$	Present
	3/7	6.00	FeTaO₄	$8.400 \pm 0.001$		$592.7 \pm 0.2$	Presen
	2/8	5.00	FeTaO₄	$8.396 \pm 0.002$		591.9 ± 0.3	Presen
			•	8.3963			(16)

TABLE III

LATTICE CONSTANTS OF COMPOUNDS

4. An increase of the lattice constant with a decrease in the oxygen partial pressure was found, which corresponds to an increase in the content of  $Ta_2O_5$ .

## The Standard Gibbs Energy of Reactions

On the basis of the established phase diagram, the standard Gibbs energies of the reactions which appear in the phase diagram can be calculated by the equation,  $\Delta G^{\circ} = -RT \ln K$ , where the R is the gas constant, the T the absolute temperature, and K the equilibrium constant of a reaction. Reactions and  $\Delta G^{\circ}$  values calculated are shown in Table IV together with the oxygen partial pressures in equilibrium. The activities of each component in the solid solutions, which are necessary in the calculations of  $\Delta G^{\circ}$ , are tabulated in the last column in Table II. The standard state was

TABLE IV The Standard Gibbs Energy of Reactions

Reaction	-log P <sub>O2</sub> (atm)	−ΔG° (kJ)
(1) $Fe + Ta_2O_5 + \frac{1}{2}O_2 = FeTa_2O_6$	15.70 ± 0.04	221.4
(2) $2FeTa_2O_6 + \frac{1}{2}O_2 = 2FeTaO_4 + Ta_2O_5$	$3.80 \pm 0.05$	6.8
(3) $FeTa_2O_6 + 3Fe + \frac{3}{2}O_2 = Fe_4Ta_2O_9$	$12.35 \pm 0.03$	522.4
(4) $Fe_4Ta_2O_9 + \frac{1}{2}O_2 = FeTa_2O_6 + Fe_3O_4$	$9.72 \pm 0.04$	133.7

arbitrarily chosen in each solid solution, as shown in Table II. Some of the details of the calculation were reported in Kimizuka and Katsura (14). The rest will be briefly described in the Appendix.

### Appendix

A phase diagram being established, activities of all components of the compounds and solid solutions have to be the same if two or three phases are stable in equilibrium. For the case of solid solutions with compositions that change with the equilibrium oxygen partial pressure, the calculation was made using the Gibbs-Duhem equation by Kimizuka and Katsura (14) and many applications were reported for the system  $Ln_2O_3-V_2O_3-V_2O_5$  by Kitayama *et al.* (17).

The method of the calculation of the activity of the Fe<sub>3</sub>O<sub>4</sub> component in the spinel solid solution will be shown as an example. Activities of iron in the wüstite solid solution were previously calculated by Darken and Gurry (12) on the basis of the Fe-O system with the Gibbs-Duhem equation. According to their results, the activity of iron at the composition ( $W_1$ ),  $a_{Fe}(W_1)$ , is  $10^{-1.545}$ , and is in equilibrium with iron in Fe<sub>3</sub>O<sub>4</sub>(M) at log  $P_{O_2} = -9.14$ . Here, the activity of iron at the composition (W) in equilibrium with pure solid Fe at log  $P_{O_2} =$ -11.94 is set at unity. The same standard was adopted in this case.

Let us consider a reaction,  $3Fe + 2O_2 = Fe_3O_4$ . Fe<sub>3</sub>O<sub>4</sub> is not in equilibrium with pure solid Fe at log  $P_{O_2} = -9.14$ , but is in equilibrium with the Fe component at the composition ( $W_1$ ). The equilibrium constant  $K = a_{Fe}^3(W_1) \times P_{O_2}^2/a_{Fe_3O_4(M)} = (10^{-1.545})^3$  $(10^{-9.14})^2$  setting  $a_{Fe_3O_4(M)}$  as unity. The same reaction is found for the end member of the spinel solid solution  $M_6$  at log  $P_{O_2} = -12.00$ . As the same reaction occurs, the constant K has to be the same in this case providing that the activity of iron is unity; that is  $K = a_{Fe}^3 \times P_{O_2}^2/a_{Fe_3O_4}(M_6)$ . Therefore,  $a_{Fe_3O_4}(M_6) = 10^{-1.09}$ .

 $a_{\text{Fe}_{3}\text{O}_{4}}(M_{4})$  was also determined using log  $P_{\text{O}_{2}} = -9.72$  and  $a_{\text{Fe}} = 10^{-1.22}$ , which is the activity of iron in the wüstite solid solution at the same  $P_{\text{O}_{2}}$  and is calculated from Darken and Gurry (12).

### Acknowledgment

The author expresses his thanks to Dr. Takashi Katsura, Emeritus Professor of Tokyo Institute of Technology, for encouragement and valuable discussions.

#### References

- 1. E. H. NICKEL, J. F. ROWLAND, AND R. C. MCADAMS, Am. Mineral. 48, 961 (1963).
- 2. T. OSAKA AND T. NAKAYAMA, Trans. Jpn. Inst. Metal 10, 437 (1969).
- R. S. ROTH, J. L. WARING, AND W. S. BROWER, J. Res. Natl. Bur. Std. A 74, 477 (1970).
- 4. J. MOREAU AND G. TRAMASURE, C.R. Acad. Sci. 258, 2599 (1964).
- 5. O. VON HEIDENSTAM, Ark. Kemi 28, 375 (1968).
- D. N. ASTROV, N. A. KRYUKOVA, R. B. ZORIN, V. A. MAKAROV, R. P. OZEROV, F. A. ROZHDEST-VENSKII, V. P. SMIRNOV, A. M. TURCHANINOV, AND N. V FADEEVA, Sov. Phys. Crystallogr. 17, 1017 (1973).
- 7. A. C. TURNOCK, J. Am. Ceram. Soc. 48, 258 (1965).
- J. L. WARING AND R. S. ROTH, J. Res. Natl. Bur. Std. A 72, 175 (1968).
- 9. N. KIMIZUKA AND T. KATSURA, J. Solid State Chem. 13, 176 (1975).
- T. KATSURA AND H. HASEGAWA, Bull. Chem. Soc. Jpn. 40, 561 (1967).
- 11. T. KATSURA AND A. MUAN, *Trans. AIME* 230, 77 (1964).
- 12. L. S. DARKEN AND R. W. GURRY, J. Am. Chem. Soc. 67, 1398 (1945).
- L. S. DARKEN AND R. W. GURRY, J. Am. Chem. Soc. 68, 798 (1946).
- 14. N. KIMIZUKA AND T. KATSURA, J. Solid State Chem. 15, 151 (1975).
- 15. V. C. KELLER, Z. Anorg. Allg. Chem. 318, 89 (1962).
- 16. J.C.P.D.S. Card No. 11-614.
- 17. K. KITAYAMA AND T. KATSURA, Bull. Chem. Soc. Jpn. 58, 948 (1985).